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Tetravalent Chromium (Cr^{4+}) as Laser-Active Ion for Tunable Solid-State Lasers

A. Seas, V. Petričević, and R. R. Alfano

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PRINCIPAL INVESTIGATOR: Prof. Robert R. Alfano

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Institute for Ultrafast Spectroscopy and Lasers
Physics Department, Room J-419
City College of New York
138 Street & Convent Avenue
New York, N.Y. 10031

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ACCOMPLISHMENTS

During 10/31/91 - 3/31/92 the following summarizes our major accomplishments made under the NASA grant: NAG-1-1346

Numerical modeling of the four mirror astigmatically compensated, Z-fold cavity was performed. The simulation revealed several design parameters to be used for the construction of a femtosecond forsterite laser.

PUBLICATIONS AND PRESENTATIONS

During the period of this report the following paper was accepted for presentation:

1. V. Petričević, A. Seas, and R. R. Alfano, "Novel Cr^{4+} -Based Tunable Solid-State Lasers", *Recent Advances in the Uses Of Light in Physics, Chemistry, Engineering and Medicine*, at City College of New York

RESEARCH PROGRAM

Modeling of a Four Mirror Astigmatically Compensated Cavity Design.

The major disadvantage of the three mirror cavity used for mode-locking of the forsterite laser^{1,2} is that when is used with long samples the beam area inside the gain medium is not uniform. This problem can be overcome by using a four mirror z-fold astigmatically compensated cavity. The z-fold astigmatically compensated cavity design takes advantage of symmetry to force the beam size in the xz and yz planes to be simultaneously minimum at the same spatial position in the laser medium³.

The z-fold four mirror cavity design is shown in figure 1. The four mirror cavity can be thought of as a combination of two three mirror cavities as shown in figure 1. One three mirror cavity consists of mirrors R_1 , R_2 , and a flat mirror positioned at the image plane and the other consists of mirrors R_4 , R_3 and the flat mirror at the image plane. Both cavities use half of the gain medium. The folding angles of the mirrors R_2 and R_3 that compensate for astigmatism can be estimated using eq.

$$2t \left(\frac{(n^2 - 1)\sqrt{n^2 + 1}}{n^4} \right) = 2f \sin \theta \tan \theta \quad (1)$$

where: t - Half the thickness of the gain medium

f - Focal length of the folding mirrors

n - Index of refraction of the gain medium

θ - Angle of incidence of the folding mirrors

Numerical calculations were performed using eq. 1 to estimate the folding angle for mirrors R_2 and R_3 to achieve astigmatic compensation in the four mirror z-fold cavity. In the calculations it was assumed that $R_2 = R_3$. Figure 2 shows the folding angle as a function of the laser crystal thickness in the case of the forsterite laser and assuming different values for the radius of curvature of the folding mirrors.

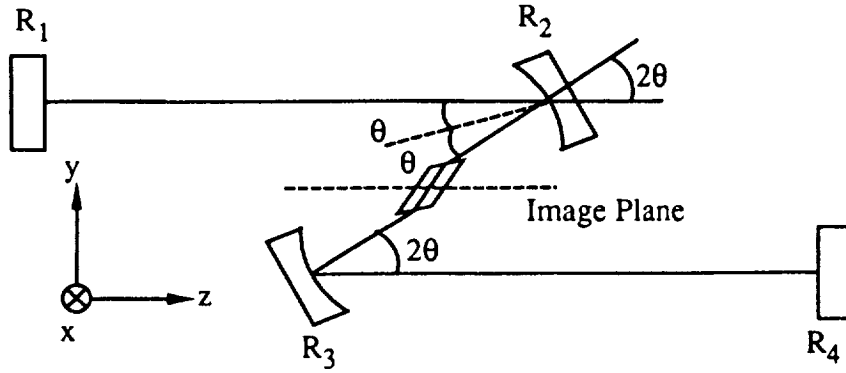


Fig. 1. Four mirror z-fold astigmatically compensated cavity design. θ is the folding angle of mirrors R_2 and R_3 .

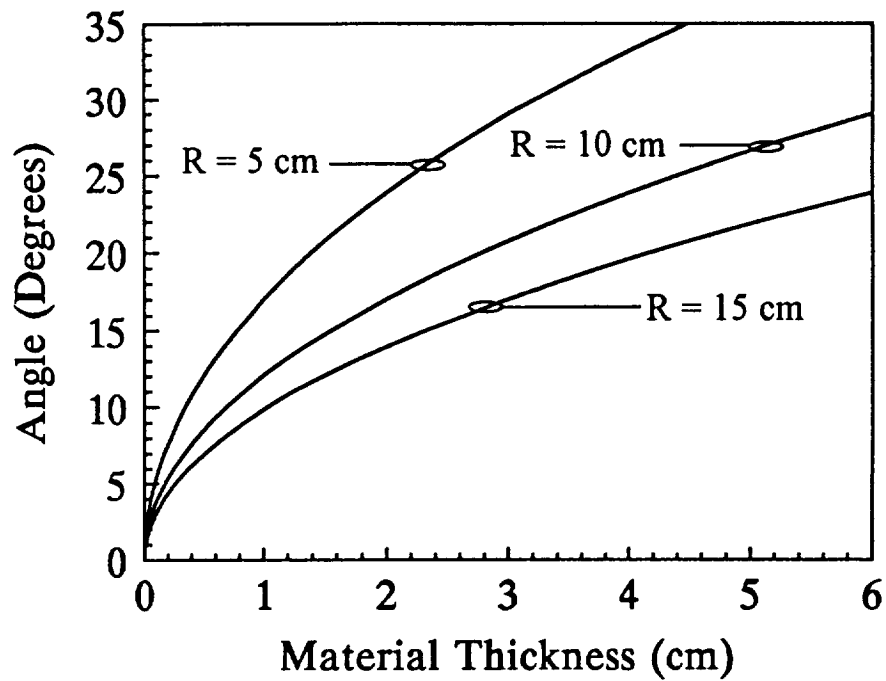


Fig. 2. Folding angle, θ , vs. forsterite crystal thickness for astigmatic compensation in a four mirror cavity.

Other characteristics of the four mirror cavity can be determined by using the theory presented in references 4 and 5.^{4,5} A computer program was developed to simulate the beam size

in the four mirror cavity used in the mode-locking experiments. For the program it was assumed that a 1 cm long chromium-doped forsterite crystal was positioned exactly at the center of the two folding mirrors R_2 and R_3 . The round trip ABCD matrix of the four mirror cavity was calculated by choosing a reference plane and following the beam for a complete round trip through the cavity (see figure 3). Note that this process was performed twice, once for the xz and once for the yz plane since the folding mirrors and the brewster-cut crystal behave differently in the two planes

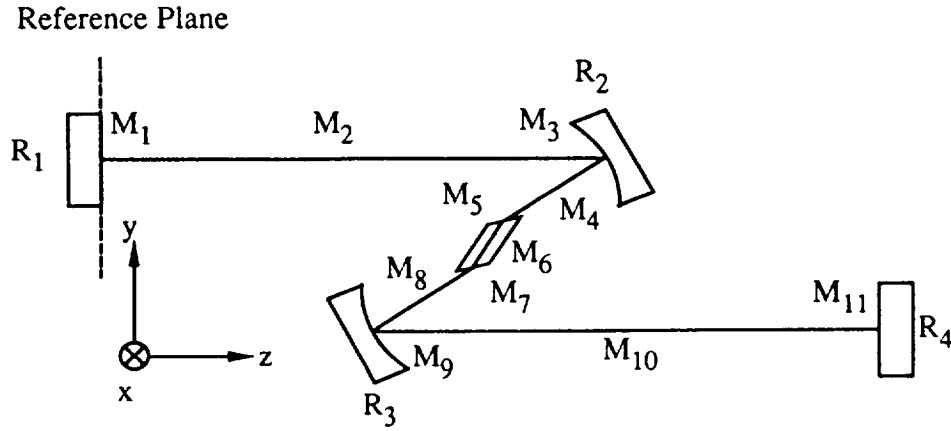


Fig. 3. Cavity configuration used in the numerical simulation.

The ABCD matrix for a complete round trip through the cavity is given by

$$M_t = M_2 M_3 M_4 M_5 M_6 M_7 M_8 M_9 M_{10} M_{11} M_{10} M_9 M_8 M_7 M_6 M_5 M_4 M_3 M_2 M_1$$

where: M_2, M_4, M_8, M_{10} - ABCD matrices for traveling a distance in free space

M_1, M_{11} - ABCD matrices for reflection from a flat mirror

M_9, M_3 - ABCD matrices for reflection from a curved mirror at an arbitrary angle of incidence (Different for the xz and yz planes)

M_5, M_7 - ABCD matrices for interface between air and forsterite crystal

M_6 - ABCD matrix for traveling in the forsterite crystal (Different for the xz and yz planes)

The stability range of the four mirror z-fold cavity design was determined next. This was done by determining the separation between mirrors R_2 and R_3 for which the self consistent and perturbation stable requirements were satisfied. The four mirror cavity is stable for $\sim \pm 1$ mm from optimum separation between mirrors R_2 and R_3 which is similar to the three mirror cavity design .

When the stability range was determined, the distance between the folding mirrors was chosen around the center of the stability range and another program was written to calculate the size of the beam waist at any point inside the resonator. This was done by moving the reference plane through out the cavity and calculating the total ABCD matrix for the new reference plane. Then the beam waist at the reference plane was estimated using eq. 2.

$$\omega_2^2 = \frac{|B|\lambda}{\pi} \sqrt{\frac{1}{1-m^2}} \quad (2)$$

where

$$m \equiv \frac{A+D}{2}$$

The results of the calculations are shown in figures 4 and 5. Figure 4 shows the size of the beam waist as a function of the position in the cavity while figure 5 is a magnified version of figure 4 showing the behavior of the beam inside the forsterite crystal. Considering figure 4 the beam waist at zero or at mirror R_1 has a value of about $600 \mu\text{m}$ and is the same for the xz and yz planes. This fact can serve as an indication when aligning the four mirror cavity. A nice round output beam is indicative of astigmatic compensation while an elliptical beam at the output indicates that the folding angle is off the optimum value. The beam waist increases from $600 \mu\text{m}$ to $800 \mu\text{m}$ as it moves 85 cm from mirror R_1 to the folding mirror R_2 . Still at mirror R_2 there is good agreement in

the size in the xz and yz planes. Mirror R_2 has a radius of curvature of 10 cm, forcing the beam to focus 5 cm away from the mirror inside the forsterite crystal. As it can be seen from figure 5 the beams inside the forsterite laser have their minimum waist at exactly the same spot. Once the beam comes out of the forsterite crystal expands rapidly up to mirror R_3 which collimates the beam. Finally the beam moves from mirror R_3 to R_4 where it gets reflected and the same transformations are repeated.

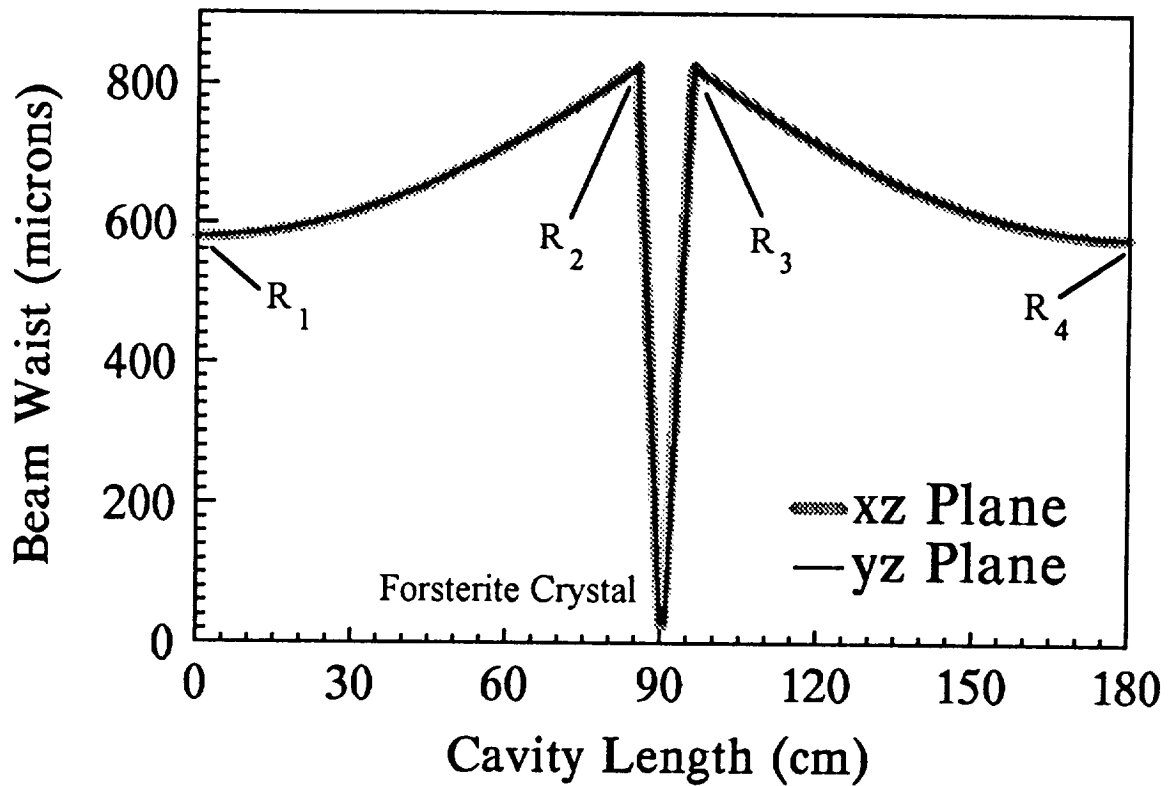


Fig. 4. Beam waist vs. position in the four mirror, z-fold, astigmatic cavity design.

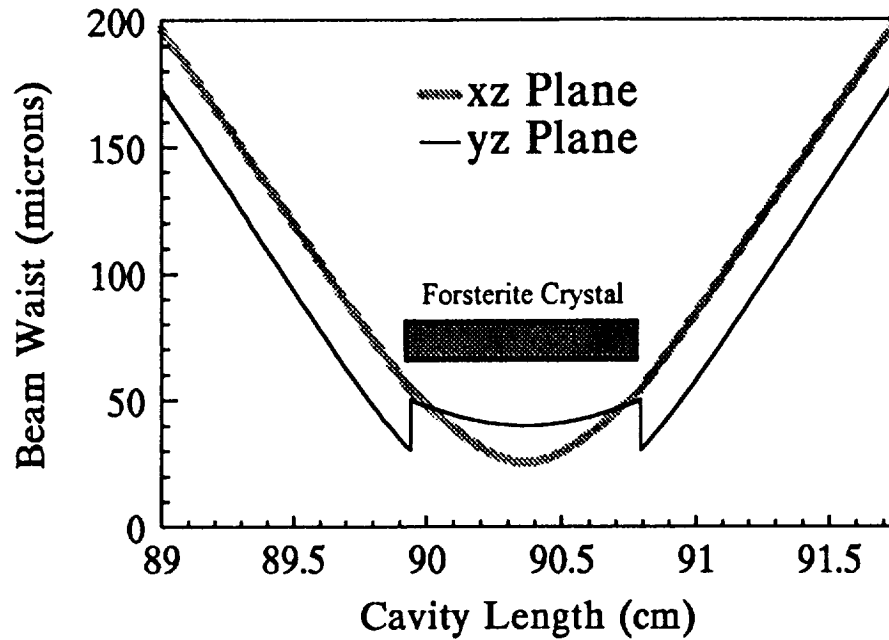


Fig. 5. Beam waist vs. position in the forsterite crystal for the four mirror, z-fold, astigmatic cavity design.

In order to be able to compare the results obtained from the analysis of the four mirror cavity design with the three mirror cavity the same computer program was modified to correspond to the three mirror cavity. For this program a 1 cm long brewster-cut forsterite crystal was placed in a three mirror cavity with $R_1 = 5$ cm, $R = 10$ cm, $R_2 = \text{flat}$ and the same procedure as with the four mirror cavity was repeated. The results of this simulation are shown in figures 6 and 7. Figure 6 shows the size of the beam waist as a function of the position in the cavity while figure 7 is a magnified version of figure 6 showing the behavior of the beam inside the forsterite crystal.

By comparing figures 5 with 7 it is clear that a four mirror z-fold cavity design has better mode characteristics as compared to the three mirror cavity. The four mirror cavity compensates for the astigmatic effects introduced by the brewster forsterite crystal and also offers a uniform mode area in the forsterite crystal. The cavity mode can be easily matched with the pump mode. In the three mirror cavity design the minimum beam waists for the two planes are formed at different positions in the forsterite crystal resulting in a non uniform mode area making hard to match pump

and cavity modes. Sub-100- μm beam size is achieved using either cavity configuration.

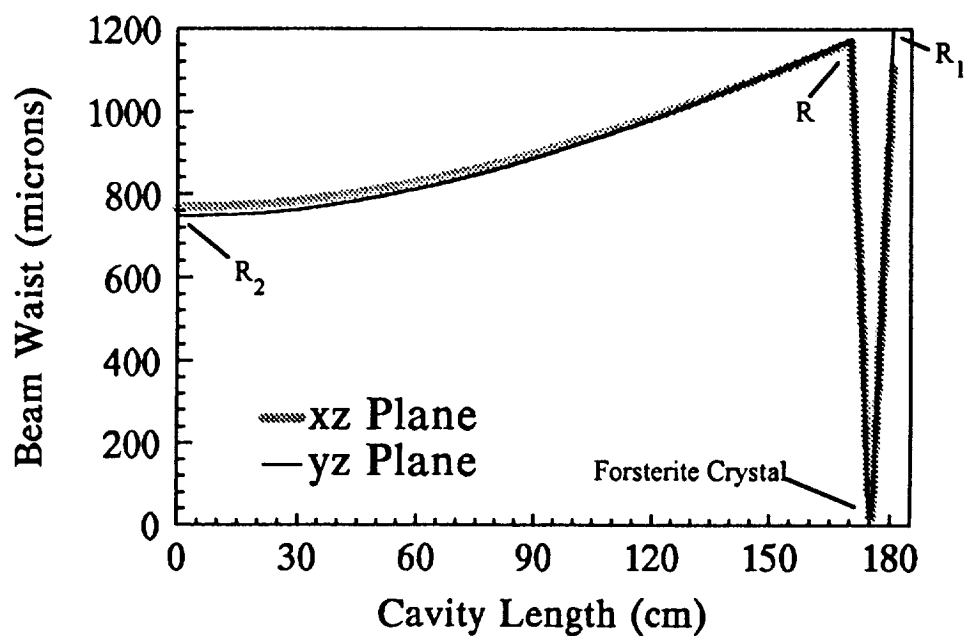


Fig. 6. Beam waist vs. position in the three mirror astigmatically compensated cavity design.

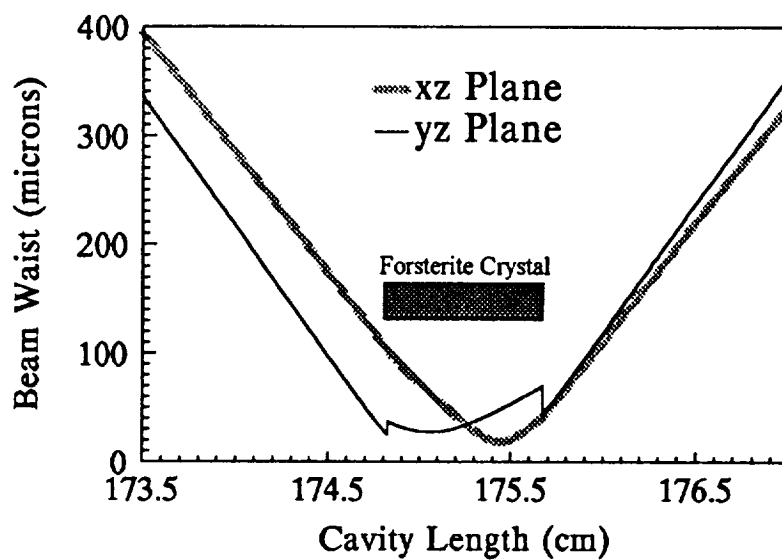


Fig. 7. Beam behavior inside the forsterite crystal in the three mirror astigmatically compensated cavity design.

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